#### RESEARCH

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# Bridging physiological and perceptual views of autism by means of sampling-based Bayesian inference

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# ABSTRACT

Theories for autism spectrum disorder (ASD) have been formulated at different levels: ranging from 10 physiological observations to perceptual and behavioral descriptions. Understanding the physiological 11 underpinnings of perceptual traits in ASD remains a significant challenge in the field. Here we show 12 how a recurrent neural circuit model which was optimized to perform sampling-based inference and 13 displays characteristic features of cortical dynamics can help bridge this gap. The model was able to 14 establish a mechanistic link between two descriptive levels for ASD: a physiological level, in terms of 15 inhibitory dysfunction, neural variability and oscillations, and a perceptual level, in terms of 16 hypopriors in Bayesian computations. We took two parallel paths: inducing hypopriors in the probabilistic model, and an inhibitory dysfunction in the network model, which lead to consistent 18 results in terms of the represented posteriors, providing support for the view that both descriptions 19 might constitute two sides of the same coin. 20

# AUTHOR SUMMARY

<sup>21</sup> Two different views of autism, one regarding altered probabilistic computations, and one regarding
<sup>22</sup> inhibitory dysfunction, are brought together by means of a recurrent neural network model trained to
<sup>23</sup> perform sampling-based inference in a visual setting. Moreover, the model captures a variety of
<sup>24</sup> experimental observations regarding differences in neural variability and oscillations in subjects with
<sup>25</sup> autism. By linking neural connectivity, dynamics and function, this work contributes to the

<sup>26</sup> understanding of the physiological underpinnings of perceptual traits in autism spectrum disorder.

# INTRODUCTION

<sup>27</sup> Autism spectrum disorder (ASD) refers to a complex neurodevelopmental condition involving

<sup>28</sup> persistent challenges in social interaction and communicative skills, and restricted/repetitive behaviors
<sup>29</sup> (Association, 2013). While some recent studies suggest that ASD could be detected during the first year
<sup>30</sup> of life in some children, early signs seem to be non-specific, with group differences more robustly
<sup>31</sup> found after children's first birthday (see Ozonoff, Heung, Byrd, Hansen, and Hertz-Picciotto (2008) for a
<sup>32</sup> review).

Almost two decades ago, John Rubenstein and Michael Merzenich suggested that many of the 33 symptoms related to ASD might reflect an abnormal ratio between excitation and inhibition leading to 34 hyper-excitability of cortical circuits in ASD subjects (Rubenstein & Merzenich, 2003). Since then, a 35 variety of studies have linked reduced inhibitory signaling in the brain with ASD symptoms, either 36 observing how behavior typically associated with ASD emerges in animals when inhibitory pathways 37 are altered, or measuring gamma-aminobutyric acid (GABA) concentration or GABA receptors in several brain regions (see Cellot and Cherubini (2014) for a detailed review). Further support for this 39 view comes from the fact that ASD patients suffer from epilepsy with a prevalence up to 25 times that 40 of the neurotypical population (Bolton et al., 2011). 41

Establishing a direct link between ASD and impaired inhibition in specific circuits in humans has not been easy. Indeed, two recent in-vivo studies in humans have shown puzzling results (Horder et al., 2018; Robertson, Ratai, & Kanwisher, 2016). In these studies inhibition was assessed both behaviorally

(in visual tasks where inhibition is widely believed to play a key role in neurotypical behavior) and by 45 measuring either GABA concentration (Robertson et al., 2016) or number of GABA receptors (Horder 46 et al., 2018) in the brains of ASD and control subjects. Interestingly, while ASD subjects showed a 47 marked deficit in binocular rivalry, characteristic of a disruption in inhibitory signaling, GABA 48 concentrations in the visual cortex were normal (Robertson et al., 2016). However, while GABA 49 concentration was predictive of rivalry dynamics in controls, the same was not true within the ASD 50 population, evidencing a disruption of inhibitory action. Similarly, while ASD subjects show an altered 51 performance in the paradoxical motion perception task (a proxy measure of GABA signaling), GABA 52 receptor availability in the brain of those participants showed no significant difference from controls 53 (Horder et al., 2018). Both studies suggest an impairment in inhibitory signaling which cannot be 54 explained by coarse differences in GABA concentration or receptor availability at the level of brain 55 areas, and which might affect specific circuits instead. To complicate matters further, there is evidence 56 for not only inhibitory but also excitatory disfunction in ASD, and it has been hypothesized that 57 homeostatic principles might be the reason behind this seemingly contradictory result (Nelson & 58 Valakh, 2015). The idea being that if, for instance inhibition is reduced, excitatory synapses might be 59 then adjusted to try to compensate for the overall change in neural activity that reduction would ensue. 60 Computational modeling of local cortical circuits expressed in terms of excitation and inhibition might 61 therefore provide a fruitful avenue of research to guide future experiments. 62

From the point of view of perception in ASD, a variety of theories have been put forward over the
last two decades. Highly influential descriptive theories include: the weak central coherence theory
(Happé & Frith, 2006) and the enhanced perceptual functioning theory (Mottron, Dawson, Soulieres,
Hubert, & Burack, 2006). Here we will focus on computational accounts of perception in ASD, and in
particular on a Bayesian view of perception (Palmer, Lawson, & Hohwy, 2017). We will later also make
connections to another influential computational theory formulated in terms of predictive coding
(Van Boxtel & Lu, 2013; Van de Cruys et al., 2014).

Within the Bayesian framework, inference about the external world proceeds by multiplicatively combining pre-existent knowledge (expressed in terms of a *prior* probability distribution) and current sensory evidence (represented in terms of a *likelihood* function), to form a *posterior* distribution which encapsulates our belief about the state of the world after having observed a given stimulus (Knill &

Richards, 1996). Rather than expressing that belief as a single point estimate of what is most probable, 74 the posterior distribution provides a richer description, naturally incorporating the associated 75 uncertainty which remains after the observation. A growing body of evidence indicates that, at least in 76 some settings, the brain is able to operate with probability distributions in this way to perform 77 approximate Bayesian inference (see Fiser, Berkes, Orbán, and Lengyel (2010), for a review). In recent 78 years it has been proposed that in ASD subjects these forms of Bayesian computations are carried out 79 abnormally: overweighting sensory evidence with respect to prior information (Palmer et al., 2017; 80 Pellicano & Burr, 2012). Concretely, the authors in Pellicano and Burr (2012) proposed that this is a 81 consequence of chronically attenuated priors (termed hypopriors), characterized by broader 82

<sup>83</sup> distributions (i.e. higher uncertainty).

The related theoretical framework of predictive coding proposes that the cortex is organized 84 following a circuit motif where feedback connections from higher- to lower-order sensory areas signal 85 predictions of lower-level responses, while feedforward connections signal errors between predictions 86 and actually observed lower-level responses (Rao & Ballard, 1999). Proponents of predictive coding 87 theories have rightfully pointed out that Bayesian theories by themselves (without specifying a 88 concrete implementation) do not offer a mechanistic explanation for ASD perception (Van Boxtel & Lu, 89 2013), which is key to understand how physiological observations may be linked to perceptual and 90 behavioral traits in ASD subjects. As has been observed by Aitchison and Lengyel (2017), Bayesian 91 inference and predictive coding are not necessarily mutually exclusive: predictive coding can be seen 92 as a computational motif which can implement several computational goals (one of which is Bayesian 93 inference), while Bayesian inference can be seen as a computational objective which can have several 94 implementations (one of which is predictive coding). Moreover, as noted in the aforementioned review, 95 telling apart the use of a Bayesian predictive coding scheme from a direct variable code in an empirical 96 setting is no trivial matter. Strong transient overshoots at stimulus onset, for instance, which are a 97 typical signature of predictive coding, can also emerge in direct variable coding schemes (Aitchison & 98 Lengyel, 2016; Echeveste, Aitchison, Hennequin, & Lengyel, 2020). Indeed, while weighting predictive 99 errors more strongly by increasing synaptic gains in the motif could explain sensory hypersensitivity 100 in ASD subjects (Palmer et al., 2017), a competing explanation can be provided within a direct variable 101 coding scheme, as we show in the present study. We note however that while predictive coding 102

- <sup>103</sup> schemes can incorporate gamma oscillations (Bastos et al., 2012), it is not clear how they would account
- <sup>104</sup> for the contrast-dependent frequency modulation of these oscillations (Roberts et al., 2013), or the
- <sup>105</sup> stimulus-dependent modulations of neural variability (Churchland et al., 2010; Orbán, Berkes, Fiser, &
- <sup>106</sup> Lengyel, 2016).



Figure 1. Sketches of the generative model, and a neural circuit implementing sampling-based probabilistic inference under that model. 107 a, The Gaussian scale mixture (GSM) generative model. Under this model, each image patch is built as a linear combination of local features (projective 108 fields), whose intensities are drawn from a multivariate Gaussian distribution. This linear combination is then further scaled by a global contrast level 109 and subject to noise. The features were in this case a set of localized oriented Gabor filters which differed only in their orientations and were uniformly 110 spread between  $-90^{\circ}$  and  $90^{\circ}$ . The image serving as stimulus in the figure is for illustration only. Photo Credit: Santa Fe Bridge by Enzo Ferrante 111 https://eferrante.github.io/) b, 2D projection of the posterior distribution for a given a visual stimulus as computed by the Bayesian ideal 112 observer under the GSM. c, The recurrent E-I neural network receives an image patch as an input, which is filtered by feedforward receptive fields matching 113 the projective fields of GSM in a. Each latent variable in the GSM is represented by the activity of one E cell in the network. d, 2D projection of the neural 114 responses of E cells corresponding the same 2 latent variables shown in b. Over time, the network samples from posterior distribution corresponding to the 115 stimulus it receives. 116

A popular implementation choice for probabilistic inference is that of probabilistic population codes (PPCs) (Ma, Beck, Latham, & Pouget, 2006), where the posterior distribution is encoded in the average rates of a population of neurons. This framework has been used in the past to link inhibitory deficits

and Bayesian computations in an artificial neural network model consisting of two feed-forward layers 120 followed by a stage of divisive normalization (Rosenberg, Patterson, & Angelaki, 2015). In this work, a 121 probabilistic version of the model was constructed to capture the "oblique effect". This term describes 122 the fact that neurotypical subjects tend to be more sensitive to cardinal than to oblique orientations in a 123 visual orientation discrimination task (Westheimer & Beard, 1998). Indeed, a modulation of the divisive 124 normalization factor in this model was shown to account for the observed reduction of the oblique 125 effect in ASD subjects (Dickinson, Jones, & Milne, 2014). The standard PPC framework requires 126 constant Fano factors (no variability modulation) (Ma et al., 2006), and furthermore feed-forward 127 network implementations can only capture mean rate responses, but fail to account for the dynamical 128 properties of neural responses that arise from recurrent connectivity. It is hence unclear in this 129 framework how altered neural variability observed in the ASD population (Haigh, Heeger, Dinstein, 130 Minshew, & Behrmann, 2015; Milne, 2011) and gamma oscillations (van Diessen, Senders, Jansen, 131 Boersma, & Bruining, 2015) would relate to probabilistic computations in these subjects. 132

Sampling-based theories for probabilistic inference offer an alternative mechanistic implementation 133 for Bayesian inference. Within this framework, neural circuits represent posterior distributions by 134 drawing samples over time from those distributions (Berkes, Orbán, Lengyel, & Fiser, 2011; Haefner, 135 Berkes, & Fiser, 2016). Interestingly, sampling-based models for probabilistic inference have recently 136 begun to establish direct links between cortical dynamics and perception (Echeveste et al., 2020). A 137 neural circuit model of a cortical hypercolumn respecting Dale's principle and performing fast 138 sampling-based inference in a visual task displayed a suite of features which are typically observed in 139 cortical recordings across species and experimental conditions. The network showed highly variable 140 responses with strong inhibition-dominated transients at stimulus onset, and stimulus-dependent 141 gamma oscillations, as observed in the cortex (Haider, Häusser, & Carandini, 2013; Ray & Maunsell, 142 2010; Roberts et al., 2013). The model further evidenced stimulus-dependent variability modulations 143 consistent with experimental findings (Roberts et al., 2013). Divisive normalization of mean responses 144 Carandini & Heeger, 2012) was also shown to emerge in this network as a result of its recurrent 145 dynamics. This is interesting since divisive normalization was precisely the starting point for the 146 probabilistic model in Rosenberg et al. (2015), and in previous work linking uncertainty and neural 147 variability via gain modulation (Hénaff, Boundy-Singer, Meding, Ziemba, & Goris, 2020). The 148

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<sup>149</sup> computational and dynamical properties of the network make it a viable candidate to test the link
 <sup>150</sup> between Bayesian computations and several physiological features observed in ASD such as inhibitory
 <sup>151</sup> dysfunction, as well as differences in neural variability and oscillations.

In what follows we will firstly set the basis for this work by recapitulating some of the key findings 152 of Echeveste et al. (2020), relating probabilistic inference, and dynamics in a network model which we 153 will take to describe healthy control subjects. We will then make use of the connection between 154 perception and physiology established by this model and take two parallel routes to explore two 155 different theories for autism: a perceptual theory expressed in terms of hypopriors, and a physiological 156 theory concerning impaired inhibition. The fist path will involve modifying the probabilistic model 157 under which perception takes place, and more concretely its prior, and observing the consequences of 158 that choice in terms of the observer's posteriors. The second path will involve inducing an inhibitory 159 deficit in the neural network whose job is to sample from the corresponding posteriors, and analyzing 160 the effect of that modification in the posteriors represented by the network. We will then compare the 161 results of both approaches to determine to what extent these two seemingly unrelated theories are 162 compatible. Finally, we show that the induced inhibitory deficit in the network model produces 163 changes in the variability and dynamics of the network. We will evaluate these changes in the context 164 of empirical observations in ASD subjects and other theoretical accounts for ASD. These include an 165 increase in neural variability, as well as an increase in the power and frequency of gamma oscillations. 166 The network also becomes hypersensitive to intense stimuli, displaying stronger transients responses 167 at stimulus onset. 168

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Inference under the GSM and responses in the original network, here representing healthy neurotypical subjects. Replotted from Figure 2. 169 Echeveste et al. (2020). In all panels shades of green correspond to the ideal observer, while red corresponds to network responses, as in Figure 1. Line colors 170 171 in b and frame colors in d indicate different contrast levels, which are the same as stimulus frames in a, indicating to which stimulus responses correspond. a, Stimuli (shade of frame color indicates contrast level, split green, blue and red indicates that the same stimuli were used as input to the ideal observer 172 and to both neural networks). b, Covariance ellipses (2 standard deviations) of the ideal observer's posterior distributions (green) and of the networks' 173 corresponding response distributions (red). Red trajectories show sample 500 ms-sequences of activities in the networks. As in the sketch of fig. Figure 1, 2D 174 projections corresponding to two representative latent variables / excitatory cells are shown. These two correspond to projective fields / receptive fields at 175 preferred orientations 42° and 16°. c, Mean (top) and standard deviation (bottom) of latent variable intensities ordered by each latent's orientation, for each 176 stimulus in the training set. Left: from the ideal observer's posterior distribution (green). Right: E cell membrane potentials u<sub>E</sub> from the networks' stationary 177 distributions (red). d, Comparison of correlation matrices. Left: for the ideal observer's posterior distributions (in green). Right: for the networks' stationary 178 response distributions (red). Response moments in  $\mathbf{c}$  and  $\mathbf{d}$  were estimated from n = 20,000 independent samples (taken 200 ms apart). Correlations in  $\mathbf{d}$ 179 are Pearson's correlations. 180

# RESULTS

#### Bayesian inference of visual features implemented by a recurrent E-I neural circuit 181

The starting point for perceptual inference within the Bayesian framework is a probabilistic model that 182 describes one's assumptions about how observed stimuli relate to variables of interest in the outside world. This forward model is usually referred to as a generative model, and the role of an ideal Bayesian 184 observer is to invert this probabilistic relationship to obtain posterior distributions over those variables 185 of interest given the observed stimulus. The generative model employed here is a Gaussian Scale-Mixture model (GSM, see Figure 1 a and Methods and Materials), which has been shown to 187 capture the statistics of natural images at the level of small image patches (Wainwright & Simoncelli, 188 2000). Importantly, inference under this model had already been shown to explain features of behavior 189 and stationary response distributions in neural data in visual perception (Coen-Cagli, Kohn, & 190 Schwartz, 2015; Orbán et al., 2016; Schwartz, Sejnowski, & Dayan, 2009). Under this version of the 191 GSM, natural image patches are constructed as linear combinations of Gabor filters of different 192 orientations, which are then scaled by a global contrast variable. The goal of the inference process was 193 to estimate the probability distribution of the intensity with which each Gabor filter (each orientation) 194 participated in the observed image. In turn, in order to model cortical neural dynamics, a common 195 recurrent neural network model is employed: the stabilized supralinear network (SSN, see Figure 1 b 196 and Methods and Materials) (Ahmadian, Rubin, & Miller, 2013; Hennequin, Ahmadian, Rubin, Lengyel, 197 & Miller, 2018). Neurons in the network were arranged around a ring, according to their preferred 198 orientation, under the approximation of visual inference problem being rotationally symmetric (though 199 see Discussion). Moreover, neurons in the network respected Dale's principle, with two separate 200 populations for excitatory (E) and inhibitory (I) cells. The SSN thus formulated was then optimized 201 using current machine learning methods to approximate a Bayesian ideal observer under the GSM: 202 when the network receives an image patch as its input, it produces samples over time with its neural 203 activity so as to represent the corresponding posterior distribution (Figure 1 c-d). Examples of the 204 image patches used to train the network, as well as sample neural trajectories are presented in 205 Figure 2 a-b, respectively. After training, posterior distributions sampled by network responses match 206 those prescribed by the ideal observer (see Figure 2 c, cf. green and red). Once trained, the SSN model 207 thus establishes a mechanistic link between neural dynamics in terms of an E-I circuit and perception 208

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formulated as sampling-based probabilistic inference. In what follows we exploit this link to take two
 complementary paths: inducing simple perturbations to the GSM to induce hypopriors, and to the SSN
 to induce an inhibitory dysfunction.

# 212 Perturbing the generative model: the effect of hypopriors

To illustrate and generate intuitions on the effect of hypopriors, we begin by employing a simplified 213 one-dimensional toy example (Methods and Materials). Let us assume the "true" prior, correctly 214 describing the statistics of the world concerning a particular inference process, is a zero-mean 215 Gaussian. Let us further assume for this toy example that the likelihood is also a Gaussian function 216 whose precision is modulated by a contrast variable which expresses the degree of reliability of the 217 sensory stimulus. If we vary the stimulus contrast we can compute a posterior distribution for each 218 stimulus under this true prior (Figure 3 a - b, in green). If, however, we were to employ a hypoprior, 219 that is a prior with a higher variance, we would obtain posterior distributions which overweight 220 sensory evidence, in the sense that they more closely resemble the likelihood function (both in mean 221 and variance) than they should. This in turn results in a higher posterior mean and in higher 222 uncertainty about the estimate (Figure 3 b, cf. green and blue lines). 223

Let us now turn to the GSM. Also in this case, a global contrast variable regulates the reliability of 224 the stimulus. However, in contrast to the 1D toy example presented before, inference in this case takes 225 place in a higher dimensional space. We again modify the prior distribution to induce a hypoprior. We 226 do so in the simplest possible way, by scaling the prior co-variance matrix by a constant factor larger 227 than 1.0 (Methods and Materials). In Figure 3 c we compare the posterior distributions calculated under 228 the true prior (in green) with those computed under the hypoprior (in blue). As expected, we again find 229 that hypopriors result in overweighting of sensory stimuli, with higher posterior means and higher 230 uncertainty about the estimates (Figure 3 d, cf. green and blue lines), consistently with the postulates of 231 Pellicano and Burr (2012). 232

#### 247 Perturbing the network: the effect of inhibitory deficits

<sup>248</sup> We now turn our attention to the network model. In what follows we will refer to the original SSN

<sup>249</sup> presented in Figure 2, as the *neurotypical* (NT) network. As previously stated, the NT-network was

- <sup>250</sup> constructed in terms of separate excitatory and inhibitory populations. Here we target inhibitory
- <sup>251</sup> connections by scaling down their efficacy by a global constant value (Methods and Materials). In order
- <sup>252</sup> to ensure that baseline activity levels are not affected, and following the ideas of Nelson and Valakh

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Effect of hypopriors on posterior predictions - GSM







Figure 3. Hypopriors and impaired inhibition. (Continues on next page)

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Figure 3. Hypopriors and impaired inhibition. a-b : Effect of hypopriors on posterior predictions for a 1D toy example. Priors, likelihoods and posteriors are all Gaussian. A contrast variable regulating the likelihood precision plays the role of the perceptual reliability of stimuli. Two example 235 inference cases are presented: under the true (well-calibrated) prior (dashed, green) and under a wider hypoprior (dashed, blue). a The prior (dashed, color) 236 and likelihood (dashed, black) are multiplicatively combined according to Bayes' rule to form the posterior (continuous, color). b Posterior mean (top plot) and standard deviation (bottom plot) under the true prior (green) and the hypoprior (blue), as a function of contrast (likelihood precision). c-d : Effect 238 of hypopriors on posterior predictions for the full multivariate GSM model. c Mean (top plots) and standard deviation (bottom plots) of latent variable 239 intensities ordered by each latent's orientation, for each stimulus in Figure 2. Left: for the well calibrated ideal observer's posterior distribution (green). 240 Right: under a hypoprior (blue). d Posterior mean (Top) and standard deviation (Bottom), averaged across all latent variables, under the true prior (green) 241 and the hypoprior (blue), as a function of contrast. e-f: Effect of impaired inhibition on network responses. e, Mean (top) and standard deviation (bottom) 242 of latent variable intensities ordered by each latent's orientation, for each stimulus in the training set. E cell membrane potentials  $u_{\rm E}$  from the stationary 243 response distributions for the NT-network (Left, red), and for the ASD-network (Right, blue). f Mean (Top) and standard deviation (Bottom) of neural 244 responses, averaged across all cells, for the NT-network (red) and the ASD-network (blue), as a function of contrast. Circles, and gray dots on x-axis of 245 panels d and f indicate training contrast levels. 246

(2015), we also scaled excitatory connections globally in a homeostatic fashion (see Supplementary 253 Fig. 1 and Methods and Materials). We will henceforth refer to the network where inhibitory deficits 254 have been induced as the ASD-network. As we did for the generative model, we then compared the 255 mean and standard deviation of the posterior distributions encoded by both networks in terms of their 256 response samples (Figure 3 e - f). Notably, we observed that ASD-network representations of the 257 posteriors also seemed to overweight current sensory information. Indeed, posterior means were 258 higher in the ASD- than in the NT-network (Figure 3 f top panel, cf. red and blue lines). In passing, we 259 note that because of the original approximate inference scheme, the scaling of the mean and standard 260 deviation with contrast between the original network and the posterior are similar but not identical. In 261 particular, while mean responses in the generative model saturate at high contrasts, they only 262 decelerate in the network model, without actually saturating. Indeed, responses in this type of network 263 models do not saturate. They either continue to grow or 'bounce back' and begin to decrease 264 (Ahmadian et al., 2013). Similarly, a slightly higher standard deviation is observed in the network with 265 respect to the posterior at low contrast, which stems from an underestimation of the variance of neural 266 responses under the Gaussian approximation during training of the network (Echeveste et al., 2020). 267

Higher uncertainty about the estimates was also found in the network (Figure 3 f bottom panel, cf.
red and blue lines), just as it happened for the generative model under hypopriors (compare Figure 3
panels d and f). Interestingly, we have reached the same qualitative traits by two very different
approaches and following two theories expressed at widely different levels: one perceptual, one
physiological.

It is important to note that sampling-based implementations of Bayesian inference establish a direct link between uncertainty and neural variability, since the width of the posterior distribution is directly related to the amount of variability. Indeed we observe that weaker inhibition leads to higher variability in the neural responses of the ASD-network compared to the NT-network (Figure 3 f,bottom panel, cf. red and blue lines), as had been suggested in Rubenstein and Merzenich (2003), where the point had been made that a disruption of E-I balance leading to a hyperexcitable cortex would lead to increased cortical 'noise'. Indeed, higher neural variability has been experimentally reported in ASD subjects both in EEG (Milne, 2011) and fMRI (Haigh et al., 2015) studies.

An advantage of employing a neural network model such as the SSN, which shows characteristic features of cortical dynamics, such as gamma oscillations and transient overshoots (including their contrast dependence), is that we can also explore the predictions the model makes for these features, now for the ASD-network.

Firstly, we look at gamma oscillations. To that end we computed the power spectrum from the local 294 field potential (LFP), from which we extracted the peak gamma frequency for different contrast levels 295 for both networks (Figure 4 a). We note that the overall frequency modulation is very similar in both 296 networks, with slightly higher peak gamma frequency in the ASD-network for high contrast stimuli 297 (cf. Figure 4 b, left panel, red and blue). Previous work has reported higher peak gamma frequency in 298 ASD subjects solving a visual task, which was interpreted as a sign of "increased neural inhibition" 299 Dickinson, Bruyns-Haylett, Smith, Jones, & Milne, 2016). At first glance, this might seem at odds with 300 the starting point for our work where we have weakened inhibitory synapses. It is worth noting 301 however that total inputs (both E and I) result in a balanced recurrent network from a dynamic 302 equilibrium, which may result in higher inhibitory currents, despite weaker inhibitory synapses. This is 303 precisely the case here (see Supplementary Fig. 1 d). Indeed, it has been known for decades that 304 balanced networks are prone to so-called "paradoxical effects" (Tsodyks, Skaggs, Sejnowski, & 305

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Transient responses and oscillations. a, LFP power as a function of frequency for stimuli of different contrast levels (same stimuli and Figure 4. 285 colors as in Figure 3) in the NT-network (left), and in the ASD-network (right). Both networks present strong gamma oscillations (see peaks in the gamma 286 band, indicated by empty circles). b, Comparison of oscillatory behavior in both networks. On the left, the peak gamma frequency is presented as a function 287 of stimulus contrast for both networks. Very minimal differences are observed. On the right, the total power within the gamma band is presented as a 288 function of contrast for both networks. A higher gamma power is observed for the ASD network at all contrasts, with strong differences at low contrasts. Across-trial average transient responses for stimuli of different contrast levels in the neurotypical network (left) and in the ASD network (righ). Both 290 networks present strong stimulus dependent transient overshoots. d, Comparison of overshoot sizes. The maximal firing rate is presented as a function 291 of stimulus contrast for both networks. We observe that the ASD network presents stronger peak responses at higher contrasts, over-reacting to intense 292 stimuli. NT-network results reproduced from Echeveste et al. (2020). 293

McNaughton, 1997), whereby direct external inhibitory inputs to I cells, can actually lead to increased I
 rates. This also hints at why seemingly contradictory results are often found regarding inhibition in
 ASD depending on what exactly is chosen as a measure of inhibition.

Interestingly however, gamma power is higher for the ASD-network (see sharper gamma peaks in
the spectra of Figure 4 a, and in Figure 4 b, right plot, blue vs red). An insight into the functional
interpretation of this effect can be obtained from analyzing neural responses at zero contrast,
representing what is usually termed spontaneous activity in the literature. In sampling based models,
such as this one, spontaneous activity is postulated to encode this prior distribution (Berkes et al.,
2011). Indeed, when the stimulus is completely uninformative, as is the case at zero contrast, the
posterior matches the prior. The model hence predicts higher gamma power in spontaneous activity,

<sup>316</sup> which is in line with previous reports of higher gamma band power in resting state activity of ASD
<sup>317</sup> subjects (van Diessen et al., 2015).

We finally turn our attention to transient responses. We compared the ASD- and NT-networks in 318 terms of their trial-averaged firing rates around stimulus onset (Figure 4 c). The model predicts higher 319 maximal firing rates (and not only mean rates) for the ASD network than for the NT network at 320 intermediate and high contrasts (cf. Figure 4 d, red and blue), indicating that the ASD-network has 321 become hypersensitive to intense stimuli. We note that theories of perception expressed in terms of 322 predictive coding usually interpret peak rates as a measure of surprise, novelty or unexpectedness (Rao 323 & Ballard, 1999), and indeed a predictive coding account of ASD perceptual traits, including abnormal 324 sensory sensitivity, has been postulated by several authors in the past (Van Boxtel & Lu, 2013; Van de 325 Cruys et al., 2014). Results from the ASD network, which we here interpret from a Bayesian inference perspective, are then not inconsistent with a predictive coding view of perceptual differences in the 327 ASD population. 328

### DISCUSSION

Neural neural network models are increasingly being used as a tool to study how differences in neural 329 architectures may be linked to symptoms in different disorders (Lanillos et al., 2020). In this work we 330 have employed a neural network model of a V1 cortical hypercolumn trained to perform 331 sampling-based probabilistic inference in a visual task to build a mechanistic bridge between 332 descriptions of ASD formulated at two very different levels: a physiological level (in terms of inhibitory 333 dysfunction (Rubenstein & Merzenich, 2003), neural variability (Haigh et al., 2015; Milne, 2011), and 334 gamma oscillations(van Diessen et al., 2015)), and a perceptual level (in terms of hypopriors in Bayesian 335 computations (Pellicano & Burr, 2012)). In what follows we describe merits of this work, limitations 336 and open questions. 337

#### **Merits**

We have taken two parallel paths: in one perturbing the probabilistic generative model in order to induce hypopriors, and in the other perturbing the neural network model to induce an inhibitory dysfunction. We observed that both approaches lead to consistent results in terms of the represented

posterior distributions, providing support for the possibility that both views of ASD might actually 342 constitute two sides of the same coin. 343

Employing a neural network model such as the SSN, which not only performs inference in a 344 perceptual task but also displays characteristic features of cortical dynamics while doing so (Echeveste 345 et al., 2020), allowed us to make further connections between characteristic differences in these dynamics and inhibitory dysfunction in ASD subjects. Stimulus-dependent variability modulations in 347 the network, and concretely the direct link between neural variability and uncertainty established by 348 sampling-based implementations of inference, predicted higher variability in neural responses in the 349 ASD- vs the NT-network. Indeed increased neural variability has been reported in ASD subjects both in 350 EEG (Milne, 2011) and fMRI (Haigh et al., 2015) studies. Moreover, transient overshoots, usually 351 interpreted in predictive coding theories to represent novelty, surprise or unexpectedness (Rao & 352 Ballard, 1999), are present in the network, with higher responses for strong stimuli in the ASD-network 353 vs the NT-network, indicating an oversensitivity to intense stimuli, a feature often reported in children 354 with ASD (Kern et al., 2006). 355

Furthermore, oscillations in the ASD-network displayed higher gamma-band oscillatory power, 356 consistent with observations in resting-state EEG recordings of ASD subjects (van Diessen et al., 2015). 357 Peak gamma frequencies were also higher in the ASD network for high-contrast stimuli, a fact which 358 has indeed been observed in EEG recordings from subjects performing an orientation discrimination 359 task (Dickinson et al., 2016), and which had been attributed to increased inhibition. We confirmed that, despite having decreased the efficacy of inhibitory synapses in our network, mean inhibitory inputs 361 were indeed actually larger for high-contrast stimuli. This observation is in line with the known fact 362 that balanced E-I networks are prone to "paradoxical effects" regarding inhibition (Tsodyks et al., 1997), 363 where average rates result from a dynamic balance of excitation and inhibition, and might explain 364 apparent contradictions between studies reporting increased/decreased inhibition (Cellot & Cherubini, 365 2014; Dickinson et al., 2016). These results also highlight the importance of neural network simulations 366 to assist in the interpretation of physiological observations regarding the role of inhibition in cortical 367 recordings. 368

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### Limitations and open questions

Training recurrent neural networks with expansive non-linearities beyond mean responses is currently 370 a challenging and computationally expensive task. These networks are prone to instabilities and 371 current optimization for second-order moments requires either a large number of trials, or 372 matrix-matrix operations which scale as  $n^3$  in the number of neurons (Hennequin & Lengyel, 2016). 373 Indeed, the choice of the simple generative model played a key role in order to make the training 374 problem tractable with currently available optimization techniques, but imposes some limitations. The 375 GSM produces multivariate Gaussian posteriors (which enabled training the network with currently 376 available second-order moment-matching methods), and was further constructed to be rotationally 377 symmetric (which drastically reduced the number of network parameters to be optimized, as well as 378 the required number of training examples). A model constructed in this way, will however not be able 379 to capture features of human behavior in popular tests of visual perception, such as the "oblique effect", where neurotypical subjects seem to be more sensitive to cardinal orientations (Westheimer & Beard, 381 1998), an effect which is reduced in ASD subjects (Dickinson et al., 2014). Tackling problems like these 382 in a sampling-based setting will require developing tools to train more flexible networks that can 383 produce richer posterior distributions. It should be noted that these limitations are however of a technical nature, and are not inherent to the sampling-based inference framework. 385

Secondly, the model employed to explain simple, low-level perceptual computations was constructed in terms of a single V1 hypercolumn, and is hence only able to capture local dynamical features, such as 387 locally generated gamma oscillations. Hypothetically, the ideas presented here can be extended to the 388 representation of other circular variables beyond orientation of visual stimuli, such as head direction in 389 rodents Skaggs, Knierim, Kudrimoti, and McNaughton (1995), motor intent in primates Georgopoulos, 390 Taira, and Lukashin (1993), physical space in grid cells McNaughton, Battaglia, Jensen, Moser, and 391 Moser (2006), or oculomotor control Seung (1998). In all these examples, highly specialized brain areas 392 receive assorted inputs that carry a noisy, filtered and distributed representation of a circular variable. 393 The recurrent activity of the network constitutes a mechanistic implementation of an inference process, 394 which could be potentially executed through a sampling-based Bayesian inference strategy, as explored 395 here. If that were the case, the strong reliance of ASD subjects on the likelihood could also be 396 broadened beyond the realm of sensory processing. Extensions of these ideas are also conceivable to 397 other one-dimensional, yet aperiodic, domains, such as sound pitch Aronov, Nevers, and Tank (2017), 398

<sup>399</sup> navigation speed Kropff, Carmichael, Moser, and Moser (2015), or elapsed time Tsao et al. (2018) which,
<sup>400</sup> although still fairly narrow in their semantic content, involve some degree of higher-level processing.
<sup>401</sup> However, as we progress into still higher cognitive functions, the understanding of how
<sup>402</sup> context-dependent modulations of cortical dynamics emerge during complex perceptual tasks will
<sup>403</sup> likely require models where multiple circuits interact (Simon & Wallace, 2016). In this sense,
<sup>404</sup> hierarchical or spatially extended versions of the SSN model employed here may provide adequate
<sup>405</sup> substrates to study inference of higher level perceptual tasks where longer-range aspects of cortical
<sup>406</sup> dynamics, such as gamma synchronization, might emerge.

Thirdly, we have focused on one aspect of probabilistic inference: inferring the state of a set of latent variables under perceptual uncertainty. The study of other aspects of this problem, such as inferring temporal transitions (Sinha et al., 2014), or causal relationships (Noel, Shivkumar, Dokka, Haefner, & Angelaki, 2021), and their link to altered inhibition and neural dynamics, will require the use of different architectures and generative models and constitute worthwhile avenues of future research.

#### 412 Closing remarks

We have shown how recurrent neural networks optimized for sampling-based inference are viable
candidates to bridge the gap between Bayesian perceptual theories of ASD and their physiological
underpinnings in terms of inhibitory dysfunction, neural variability and oscillations. We believe these
results highlight the potential for the use of the emerging body of function-optimized neural networks
(Echeveste et al., 2020; Hennequin, Vogels, & Gerstner, 2014; Orhan & Ma, 2017; Remington, Narain,
Hosseini, & Jazayeri, 2018; Song, Yang, & Wang, 2016; Yamins et al., 2014) as models to establish
mechanistic links between neural activity and computations in the cortex that go beyond the study of
neurotypical perception.

# **METHODS**

In order to link cortical dynamics and probabilistic computations we modified the parameters of the
probabilistic and network models employed in Echeveste et al. (2020). In what follows we describe
those changes and refer the reader to the original paper for a more detailed description of the models
and of the original model parameters.

#### 425 The generative model

In this work the Gaussian scale mixture model (GSM, Wainwright and Simoncelli (2000)), is employed
as the generative model of natural images (at the level of small patches) under which inference is
carried out in the primary visual cortex (V1, Coen-Cagli et al. (2015); Orbán et al. (2016)). Under the
GSM an image patch x is obtained by linearly combining a number of local features (given by the
columns of a matrix A), which are weighted by a corresponding number of feature coefficients given by
y, further scaled by a single contrast variable *z*, and finally corrupted by additive white Gaussian noise.
This forward generative model can then be summarized in terms of the likelihood function given by

$$\mathbf{x}|\mathbf{y}, z \sim \mathcal{N}(z \, \mathbf{A} \, \mathbf{y}, \sigma_{\mathbf{x}}^2 \, \mathbf{I}),$$
 (1)

together with the priors for the feature coefficients and the contrast variable z. Local features were assumed to be drawn from a multivariate Gaussian:

$$\mathbf{y} \sim \mathcal{N}(\mathbf{0}, \mathbf{C}),$$
 (2)

and the contrast was assumed to be drawn from a Gamma prior. To induce hypopriors we modified the overall scale of the prior covariance matrix **C**, by taking  $\mathbf{C}_{HP} = \alpha_{HP}\mathbf{C}$ , with  $\alpha_{HP} = 1.5$ . Other values were explored without qualitative differences (not shown). We note that taking  $\alpha_{HP} > 1$  results in wider priors, as required for a hypoprior.

The 1D toy example model of Figure 3a–b, corresponds to a 1-dimensional GSM with prior variance C = 4, A = 10, and  $\sigma_x^2 = 100$ . As in the full GSM, we took  $\alpha_{\text{HP}} = 1.5$ .

#### <sup>41</sup> Network dynamics and architecture

The circuit model consisted of a nonlinear, stochastic network respecting Dale's principle, with  $N_{\rm E}$ excitatory and  $N_{\rm I}$  inhibitory neurons. The evolution of the membrane potential  $u_i$  of each neuron i in this model is described by (Hennequin et al., 2018)

$$\tau_i \frac{du_i}{dt} = -u_i(t) + h_i(t) + \sum_j W_{ij} r_j(t) + \eta_i(t) , \qquad (3)$$

where  $\tau_i$  represents the membrane time constant for neuron *i*,  $h_i$  its feedforward input, and  $\eta_i$  is the process noise (capturing both intrinsic and extrinsic forms of neural variability). W is the matrix of

recurrent connections, and hence  $W_{ij}$  represents the strength of the synapse connecting neuron j to neuron i. As previously mentioned, the network is non-linear, with firing rates

$$r_i(t) = k \lfloor u_i(t) \rfloor^m.$$
(4)

Here k and m represent the scale and exponent of the firing rate nonlinearity (Ahmadian et al., 2013). 449 Given the rotational symmetry of the problem, W itself was parametrized to be rotationally symmetric. 450 Neurons in the model are arranged in a ring of pairs of E and I cells according to their preferred 451 orientations (Figure 1c) where  $W_{ij}$  was a smoothly decaying function of the tuning difference between neurons i and j (see Supplementary Fig. 1 a, top and second row). The (stimulus-independent) process 453 noise covariance was analogously parametrized (see Supplementary Fig. 1 a, third row). Following 454 canonical models of V1 simple cells (Dayan & Abbott, 2001), feedforward inputs to the network were computed by applying a linear filter  $\mathbf{W}^{\mathrm{ff}}$  to the stimulus (the image patch) followed by a nonlinearity 456 (see Supplementary Fig. 1 a, bottom row). 457

The perturbation here employed to induce an inhibitory deficit has a single free parameter  $\delta_{\rm I}$  which scales the inhibitory columns of  $\mathbf{W}$ ,  $\mathbf{W}_{\rm I}^{\rm ASD} = (1 - \delta_{\rm I})\mathbf{W}_{\rm I}^{\rm NT}$  (see Supplementary Fig. 1 a–b). In order to maintain the baseline level of activity, a second modification is introduced (simulating homeostatic adaption of the excitatory connections), scaling the excitatory columns of  $\mathbf{W}$  by a factor  $\delta_{\rm E}$ :  $\mathbf{W}_{\rm E}^{\rm ASD} = (1 - \delta_{\rm E})\mathbf{W}_{\rm E}^{\rm NT}$ . This second factor was found by grid-search minimization of the homeostatic cost

$$\mathcal{C}_{\rm h} = \left| \mu_{\rm s}^{\rm NT} - \mu_{\rm s}^{\rm ASD} \right|,\tag{5}$$

<sup>464</sup> capturing the change in mean spontaneous activity levels ( $\mu_s$ ) between the original NT- and perturbed <sup>465</sup> ASD-network . This adaptation procedure returns a single  $\delta_E$  value for each  $\delta_I$  value (Supplementary <sup>466</sup> Fig. 1 c). We note that excitatory changes via this procedure resulted always smaller than inhibitory <sup>467</sup> ones (cf. to identity line in Supplementary Fig. 1 c, bottom plot). Network results presented throughout <sup>468</sup> this paper correspond to  $\delta_I = 0.1$ , for which  $\delta_E = 0.076$ . Numerical experiments were repeated for <sup>469</sup>  $\delta_I = 0.05$  and  $\delta_I = 0.15$  without qualitative differences (not shown).

Stationary moments of neural responses to a fixed input (Figure 3e) were computed from 20,000 independent samples (200 ms apart) generated by letting neural activity in the network evolve over time via Equation 3 (excluding transients). Power spectra in Figure 4 a were obtained from simulated local field potentials (LFPs), computed as the average (across-cells) membrane potential. Gamma peak frequencies in Figure 4 b (left) were obtained as the local maximum in the spectrum within the gamma range (20–80 Hz), while total gamma power in Figure 4 b (right) was computed as the integral of the spectrum over that same range.

Transient responses displayed in Figure 4 c were computed as the mean (across E-cells and trials) firing rates (n = 100), which are then further averaged over a 10-ms sliding window. A random delay time (sampled from a truncated Gaussian, with a mean of 45 ms and a standard deviation of 5 ms) was employed for the feedforward input to each pair of E–I cells. These procedures had been put in place to allow for a comparison to experimental data, and are here kept in order to compare the ASD-netowork to replotted results from the original (here NT-) network. Maximal firing rates in Figure 4 d were obtained as the peak rates from transient firing rate responses.

#### 485 Code availability.

- The (Python) code to create the ASD network is provided in
- <sup>87</sup> bitbucket.org/RSE\_1987/inhibitory\_dysfunction. The code for the numerical
- 488 experiments can be found at:
- bitbucket.org/RSE\_1987/ssn\_inference\_numerical\_experiments.

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- <sup>492</sup> potential avenue of research after discussing previous work.

### **TECHNICAL TERMS**

- <sup>493</sup> Latent variable A variable of interest to which an observer has no direct access and hence needs to
- <sup>494</sup> infer it from an observation of other related variables.

Prior Probability distribution encapsulating an observer's knowledge about the latent variables
 before observing the stimulus.

Likelihood function Function describing the conditional probability of an observation for each
 state of the latent variables.

<sup>499</sup> **Posterior** Conditional probability over the latent variables after observing a given stimulus.

Hypoprior A chronically attenuated prior, whose uncertainty is higher than implied by the statistics
 of stimuli.

<sup>502</sup> GABA Main inhibitory neurotransmitter.

Gamma Oscillations Rhythmic patterns of activity with a frequency between 20 and 80Hz.

Transient overshoot Excursion in neural responses that exceeds mean responses over a brief period of time after the onset of the stimulus.

<sup>506</sup> **Divisive normalization** Process by which the responses of single neurons are divisively modulated <sup>507</sup> by the responses of other neurons.

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